Math 31B — Homework 01

Instructions Remember to show all of your work to get credit. Please do this assignment on a seperate sheet of paper. The assignment is due at the beginning of class on Friday.

- 1. 7.3: 113
- 2. 7.3: 95, 98, 103
- 3. 7.1: 53, 54
- $4.\ 7.1\ 81,\ 82$
- 5. (a) Using of the definition of the derivative show that

$$\frac{d}{dx}\left[b^x\right] = m(b)b^x$$

where

$$m(b) = \lim_{h \to 0} \frac{b^h - 1}{h}.$$

- (b) What is the exact value of m(b).
- 6. Find an inverse function for $f(x) = x^2 + 1$ when $x \ge 1$.
- 7. Consider the function

$$l(x) = \int_1^x \frac{c^2}{t} dt$$

where c is a constant. What is the base of this logarithm?

- 8. Consider the logarithm $l(x) = 2 \log_5(x)$. What is the base of this logarithm?
- 9. What is the hyperbola associated to the logarithm $\log_{10}(x)$? How about $\log_a(x)$ where a is a positive real number bigger than one?.
- 10. What is the derivative of $\ln(x)$? What is the derivative of $\log_{10}(x)$? What is the derivative of $\log_a(x)$?
- 11. (For fun) Go find an unsuspecting victim (if you live in a dorm there should be many) and ask them to solve the equation $e^x + x = y$ for x.